

2+4

```

mov rax, 4
mov [rbp-8], rax
mov rax, 8
mov [rbp-16], rax
mov rax, [rbp-8]
add rax, [rbp-16]

```

Registers we have used

rax, r10, r11, rsp, rdi, rbp

Access Speed (approx)

register	1 clock cycle
L1 cache	~4 clock
L2 cache	~10 clock
L3 cache	~40 clock
RAM	~100-300

## Register Allocation

```

let a = 2+4 in
let b = 3-1 in
let c = a+b in
let d = b+1 in
let e = 5 in
let f = d+2 in
let g = e+f in
g

```

8 ↗

(1b) (4b) (5b)

```

mov rax, 4
add rax, 8      r12
mov [rbp-8], rax
mov rax, 6
sub rax, 2      r13
mov [rbp-16], rax
mov rax, [rbp-8] r12
add rax, [rbp-16] r13
mov [rbp-24], rax r14
mov rax, [rbp-16]
add rax, 2      r13
mov [rbp-32], rax r15
mov rax, 10      [rbp-8]
mov [rbp-40], rax
mov rax, [rbp-32]
add rax, 4
mov [rbp-48], rax
mov rax, [rbp-40]
add rax, [rbp-48]
mov [rbp-56], rax
mov rax, [rbp-56]

```

(1) Greedy allocation algorithm

(-8, { })

[rbp-8], [rbp-16], [rbp-24], ...

(-8, [ArgRegister R12; ArgRegister R13;  
... ], { })

r12, r13, r14, r15, [rbp-8], ...

(2) Linear Scanning

\* when running out of registers:  
swap some reg value into stack memory  
and re-use register

produce code ~30% - 40% slower than alg used in tools like clang  
runs very fast (in compiler) — good for JIT

```

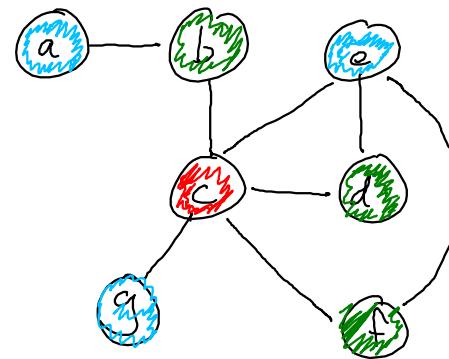
let a = 2 + 4 in ]
let b = 3 - 1 in ]
let c = a + b in ]
let d = b + 1 in ]
let e = 5 in ]
let f = d + 2 in ]
let g = e + f in ]
g + c

```

“variable liveness”

Graph coloring  
NP-hard

r<sub>12</sub>  
r<sub>13</sub>  
r<sub>14</sub>



## Graph Coloring

Interference Graph:

vertices : variables (conceptual storage)

edges : coexistence

color : physical storage

Solution =  
find a mapping

$M: V \mapsto C$  such that

- (1) If  $\langle V_1, V_2 \rangle \in E$ ,  
then  $M(V_1) \neq M(V_2)$
- (2) minimal codomain of  $M$   
(fewest colors possible)

Polynomial time approximation

## Intermediate Representation

```

mov rax, 4
add rax, 8
mov LOC1, rax
mov rax, 6
sub rax, 2
mov LOC2, rax
mov rax, LOC1
add rax, LOC2
mov LOC3, rax
mov rax, LOC2
add rax, 2
mov LOC4, rax
mov rax, 10
mov LOC5, rax
mov rax, LOC4
add rax, 4
mov LOC6, rax
mov rax, LOC5
add rax, LOC6
mov LOC7, rax
mov rax, LOC7

```