

Hash Table

- Data structure has average $O(1)^*$ complexity for Dictionary operations (get, insert, update, remove)
- Backed using array
- (Tricks from Array List will be helpful)
- Each slot in array has a key-value mapping and some way of determining if the slot is in use
- (not interpreted as a tree)
- hash function $K \mapsto \text{int}$ (should evenly distribute keys)
- Use hash of each key to decide where to put mapping
- Collision: when two keys want to be in the same slot (according to hash)

insert(1, "a")
insert(7, "b")
insert(5, "c")

K		5		7
V		"c"		"b"
bool	x	✓	x	✓

- One collision resolution strategy: (Linear probing)
 - Just use next slot
 - On get: check next slot too until I find it or slot is empty
 - On remove: check next slots to move collided keys back
- To prevent frequent collisions:
 - Calculate "load factor" $LF = \frac{\# \text{ mappings}}{\# \text{ slots}}$
 - If adding a mapping would increase LF beyond "max load factor", then double array size & rehash all mappings
 - Common MLF $\approx 1/2, 3/4, 2/3$

Collision resolution strategy: forward chaining

Linear Dictionary: dictionary backed by ArrayList (not sorted)
get/insert/update/remove

Method get (K key):

```

For each index i:
  If contents.get(i).first == key:
    Return contents.get(i).second
  EndIf
EndFor
  
```

EndMethod

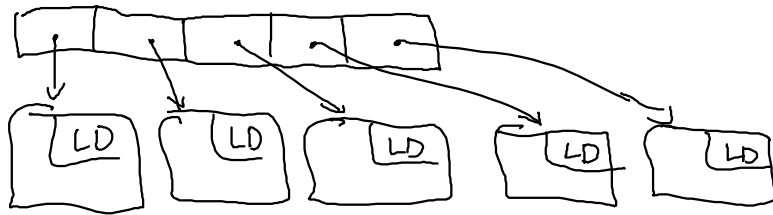
Method insert (K key V value):

```

For each index i:
  If contents.get(i).first == key:
    11
  EndIf
EndFor
contents.insertLast((key, value))
EndMethod
  
```

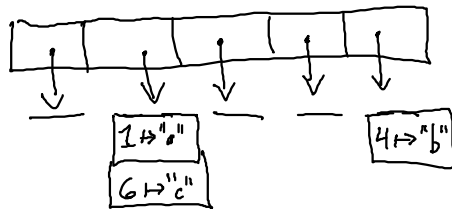
Forward chaining:

Hash table contains an array of Linear Dictionary objects

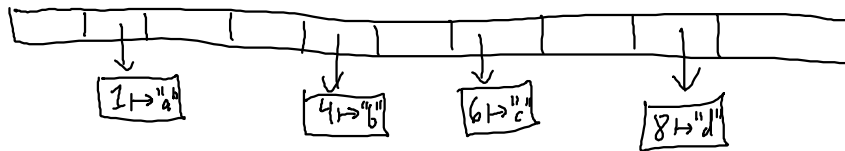


$MLF = 3/4$

insert (1, "a")
insert (4, "b")
insert (6, "c")
→ insert (8, "d")



exceed
MLF: rehash everything



Hash table insert: WC $O(n)$

amortized average $O(1)$

expected (over chance)
amortized (over a sequence)
?? (over all possible inputs - keys)

There is always a set of keys that makes a HashTable give $O(n)$ performance